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Instructional video 1
Now let's see how to construct a locus of equi-angular points, in this case, the locus of all points X such that angle AXB is $75^{\circ}$ and the measure of line segment AB is 5 cm . From the point of view of geometric constructions, we are looking for the locus of all points X at the circumference of a circle such that the angles with vertices $X$ subtended by line segment $A B$ are $75^{\circ}$.

At first, we need to draw a line segment AB which is 5 cm . Secondly, we construct the angle which is $75^{\circ}$ such that the line segment AB is one of the arms of this angle and the vertex is either at point A or B. In our case it's point B. The other arm of the angle will be line $t$.

Thirdly, we need to construct a perpendicular to line $t$ at point $B$ and then we also construct a perpendicular bisector of AB .

The point of intersection of the perpendicular bisector and the perpendicular is the centre of the required circle.

Finally, we draw a circle with centre S and radius SA or SB.
The required locus of equi-angular points is the arc of the circle $A B$ lying in half-plane ABS.
In this construction we have used the properties of inscribed, central and tangent-chord angles.

Instructional video 2
How to construct a locus of equi-angular points if an angle AXB is an obtuse angle.
At first, we need to draw the given line segment which is 5 cm .
Secondly, we construct the angle which is $110^{\circ}$ such that the line segment AB is one of the arms of this angle and the vertex is either at point A or B , in this case it's point B . The other arm of the angle will be line t .

Thirdly, we construct a perpendicular to line $t$ at point $B$ and then, we also construct perpendicular bisector of AB.

The point of intersection of the perpendicular bisector and the perpendicular is the centre of the required circle.

Finally, we draw a circle with radius SA or SB.
In this case, the required locus of equi-angular points is the arc of the circle $A B$ lying in a half-plane opposite to half-plane ABS.

